

# Physics-Based Decomposition of Reflectance and Shading using a Single Visible-Thermal Image Pair

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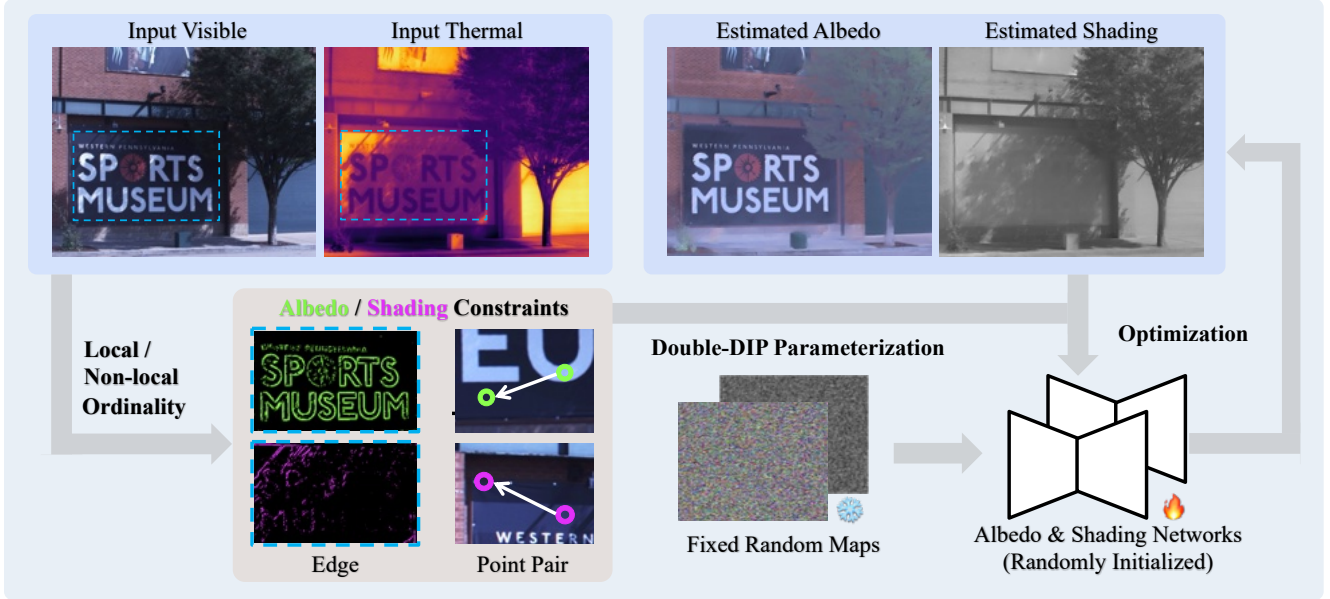


Figure 1. Through the tree’s veil, sunlight weaves intricate shadows across a building façade. Visible and thermal images capture complementary cues of reflected and absorbed light. Local and non-local visible–thermal ordinalities (Sec. 3) reveal albedo/shading edges and point-pair ordinalities respectively, guiding an optimization using Double-DIP parameterization (Sec. 4). Our physics-based method reconstructs the complex shading and albedo without learned priors, whereas state-of-the-art models fail (see supplementary).

## Abstract

Decomposing an image into its underlying photometric factors—surface reflectance and shading—is a long-standing challenge due to the lack of extensive ground-truth data for real-world scenes. We introduce a novel physics-based approach for intrinsic image decomposition using a pair of visible and thermal images. We leverage the principle that light not reflected from an opaque surface is absorbed and detected as heat by a thermal camera. This allows us to relate the ordinalities (or relative magnitudes) between visible and thermal image intensities to the ordinalities of shading and reflectance, which enables a dense self-supervision of an optimizing neural network to recover shading and reflectance. We perform quantitative evaluations with known reflectance and shading under natural and artificial lighting, and qualitative experiments across

diverse scenes. The results demonstrate superior performance over both physics-based and recent learning-based methods, providing a path toward scalable real-world data curation with supervision.

## 1. Introduction

Understanding how a scene appears from the interaction between surface reflectance and incident illumination has long been a central pursuit in vision and imaging sciences [3]. Disentangling these physical factors is useful for various applications in graphics (recoloring, relighting, and compositing) and vision (object recognition and tracking). Recent learning-based methods have made progress by formulating this task in an end-to-end framework and inferring statistical priors from auxiliary datasets to constrain the otherwise ill-posed inverse problem [17]. However, collecting ground-truth data for real-world scenes remains infeasible,

as measuring surface reflectance and shading requires specialized equipment and controlled procedures [19, 41].

In this paper, we introduce a novel physics-based framework that leverages a single auxiliary thermal image to decompose a visible image of a scene into its albedo and shading components. To see why a thermal image is useful here, we consider the underlying physical principles that govern albedo and shading. Shading corresponds to the total incident energy (or irradiance) at a scene point, while albedo represents the proportion of that energy reflected by the surface. For opaque objects, the unreflected portion of the incident energy is absorbed, which contributes to the thermal radiation. This radiation can be detected by a thermal camera in the long-wave infrared range (8–14  $\mu\text{m}$ ). However, directly estimating the absorbed light is challenging without prior knowledge of the surface albedo. A recent technique called JoLHT-Video [33] addressed this issue by modeling heat generation using heat transport equations and estimating it from the heat flow observed in a thermal *video*. Inspired by their work, we pose the following question: *What can be achieved using only a single thermal image?*

Since absorption of light increases the temperature of an object, low-albedo regions—dark in the visible image—appear bright in the thermal image, whereas shading variations appear bright in both. Based on this observation, we relate visible–thermal intensity ordinalities between any two scene points to their albedo and shading ordinalities, *without* having to estimate the absorbed light. Specifically, the ordinality of neighboring scene points classify edges into shading vs. reflectance and define an edge loss, while non-local ordinalities yield a point-pair loss. These new losses are used alongside the standard visible image reconstruction loss to optimize a neural network (e.g. Double Deep Image Prior [16]), effectively providing dense self-supervision to recover shading and albedo.

Our ordinality theory is derived using the Lambertian assumption and when illumination is confined to the visible spectrum (e.g., LED lighting). We further extend it to broadband sources containing infrared energy (e.g., sunlight, incandescent bulbs) by empirically observing that infrared albedo exhibits lower spatial variation than visible albedo [9], thereby preserving ordinalities. Expert validation on diverse materials and natural scenes—including those moderately violating the Lambertian assumption—shows near-perfect agreement between our automatically estimated point-pair ordinalities and confident expert labels, confirming robustness across material types and generalization beyond idealized conditions.

We quantitatively evaluate our method on scenes with known reflectance (e.g. color charts) and known shading (e.g. object imaged under identical lighting but painted differently). We further test on visible–thermal pairs simulated from the MIT Intrinsic dataset [19]. Finally, we demon-

strate qualitative results on complex indoor and outdoor scenes with notable improvements over both physics-based and learning-based methods trained on auxiliary datasets. Our VT-Intrinsic dataset of visible–thermal image pairs can offer supervision for learning methods in real-world scenes.

## 2. Related Work

### 2.1. Thermal Imaging for Physics-Based Vision

Thermal cameras have recently emerged as a powerful complement to visible sensing across geometry [31, 32, 38], materials [12], and appearance [2]. In intrinsic image decomposition, JoLHT-Video [33] showed that transient thermal video captured under controlled illumination provides analytical cues for estimating absorbed and reflected light. In contrast, our method relies on a *single* thermal image to extract reliable ordinal constraints on albedo and shading without the demand of video or lighting.

### 2.2. Intrinsic Image Decomposition (IID)

Owing to their ill-posed nature, intrinsic image decomposition methods generally fall into three categories.

*Early optimization-based approaches:* Retinex-style [24] methods rely on stringent assumptions that hinder generalization—such as smooth shading or reflectance [4], chromaticity-preserving shading variations [11, 14, 18], or local intensity similarity implying shared reflectance [36].

*Learning-based approaches:* Unsupervised learning based methods that decorrelate albedo and shading [28] or that enforce albedo consistency across changing illumination [26] improve upon hand-crafted priors. Supervised learning-based models are primarily trained on synthetic datasets [23, 25, 27, 34], which provide ground-truth albedo and shading but face a significant sim-to-real gap. Existing real-world datasets [5, 22, 41] offer sparse annotations used by models (e.g., to predict albedo ordinalities [43]), but are limited to small-scale indoor scenes. Intrinsic-v1 [6] expands to more diverse data by using model predictions as pseudo-ground truth, albeit imperfectly. Recent works [21, 29, 42] leverage diffusion priors for IID, yet as noted in [7], they suffer from hallucination.

*Using auxiliary sensors:* Cheng et al. [8] used near-infrared (NIR) images as shading proxies, but NIR albedo often varies across materials (albeit less than visible) and modern efficient lighting such as LEDs hardly emits NIR, limiting generality and applicability. Sato et al. [35] used intensity of sparse LiDAR returns and enforce consistency with estimated albedos, yet LiDAR operates in NIR where albedo differs from visible [8]. While such NIR cues help in specific cases, our approach exploits the complementary relation between visible (reflected light) and thermal (proxy for absorbed light), enabling broader applicability.

### 3. Theory of Visible-Thermal Ordinality

We present the theoretical relationship between a visible and thermal image pair and show that the ordinality of their pixel intensities directly convey the ordinality of the underlying albedo or shading, as illustrated in Fig. 2. We first consider visible illumination (e.g., an LED), then extend our analysis to include invisible illumination (e.g., infrared light). While we develop the theory for a grayscale visible camera, the results can be adapted to multiple color channels, as shown in Section 4.

#### 3.1. Visible-only Illumination

Consider an opaque Lambertian scene imaged by visible and thermal cameras. The visible intensity at a pixel  $x$  is:

$$I_v(x) = g\rho(x)\eta(x), \quad (1)$$

where  $\rho$  is the albedo (reflectance),  $\eta$  the shading (irradiance), and  $g = k/\pi$  a global scale determined by the camera gain  $k$ . For brevity, we omit  $x$  denoting a single pixel.

Light not reflected is absorbed by the surface and converted into heat, producing a heat source of intensity:

$$\mathcal{H} = (1 - \rho)\eta. \quad (2)$$

This heat propagates through conduction, convection and radiation according to the heat transport equation. Though  $\mathcal{H}$  is not directly measurable, it can be inferred from surface temperature, which is indirectly observed by a thermal camera. JoLHT-Video [33] modeled the light-heat transport using thermal video of the heating process to estimate  $\mathcal{H}$  and solve for  $\rho$  and  $\eta$ . In contrast, we use a single thermal image  $I_t$  near thermal equilibrium, easily attainable within seconds under stable lighting, as described in Sec. 3.3.

Together,  $I_v$  and the absorbed heat image  $\mathcal{H}$  impose local and non-local constraints on albedo and shading.

##### 3.1.1. Local (Edge) Constraints

The spatial gradient of the visible image can be written as:

$$\nabla I_v = g(\nabla\rho)\eta + g\rho(\nabla\eta). \quad (3)$$

For most edges in natural images, one of the two terms on the right dominates—edges arise primarily from either albedo or shading variations [18, 24]. This creates a fundamental ambiguity, but the spatial gradients of the heat source provide complementary information:

$$\nabla\mathcal{H} = (-\nabla\rho)\eta + (1 - \rho)\nabla\eta. \quad (4)$$

From (3) and (4), note that

$$\text{Albedo Edge}(\nabla\eta \rightarrow 0): \text{sign}(\nabla I_v) = -\text{sign}(\nabla\mathcal{H}), \quad (5a)$$

$$\text{Shading Edge}(\nabla\rho \rightarrow 0): \text{sign}(\nabla I_v) = \text{sign}(\nabla\mathcal{H}). \quad (5b)$$

This yields a simple criterion to distinguish albedo- and shading-dominant edges using the heat intensity image.

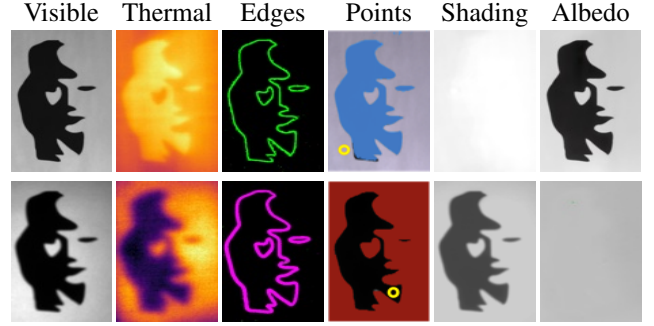


Figure 2. Printed (top) vs. projected (bottom) Roger Shepard’s illusion [37]. **Top:** a *printed* paper lit by an incandescent bulb, where reflectance variations reveal a saxophone player. **Bottom:** the same pattern *projected* onto a uniform cardboard, where modulated shading reveals a lady’s face. This comparison highlights the albedo-shading ambiguity and motivates modeling light-heat transport: reflectance induces inverse visible-thermal ordinalities, while shading yields consistent ones. Columns 3-4 show classified albedo- / shading-dominant edges (Sec. 3.1.1) and points of lower albedo / higher shading than  $\odot$  (Sec. 3.1.2). Our method decomposes correctly (right), whereas baselines fail (see supplementary).

##### 3.1.2. Non-Local (Point-Pair) Constraints

We generalize the above gradient analysis to compare point pairs, i.e., any two distinct pixels  $x_i$  and  $x_j$  in the scene.

$$I_v(x_i) = g\rho(x_i)\eta(x_i), \mathcal{H}(x_i) = (1 - \rho(x_i))\eta(x_i), \quad (6a)$$

$$I_v(x_j) = g\rho(x_j)\eta(x_j), \mathcal{H}(x_j) = (1 - \rho(x_j))\eta(x_j). \quad (6b)$$

When a pixel’s visible intensity is lower (or higher) than another’s while its thermal intensity is higher (or lower), the pixel’s albedo is correspondingly lower (or higher).

**Proposition 1 (Albedo Ordinality).** *Given two pixels,  $x_i$  and  $x_j$ , with visible and heat intensities as in (6), if  $I_v(x_i) < I_v(x_j)$  and  $\mathcal{H}(x_i) > \mathcal{H}(x_j)$ , then  $\rho(x_i) < \rho(x_j)$ , and vice versa.*

Conversely, when both visible and thermal intensities are lower (or higher), its shading is also lower (or higher).

**Proposition 2 (Shading Ordinality).** *Given two pixels,  $x_i$  and  $x_j$ , with visible and heat intensities as in (6), if  $I_v(x_i) < I_v(x_j)$  and  $\mathcal{H}(x_i) < \mathcal{H}(x_j)$ , then  $\eta(x_i) < \eta(x_j)$ , and vice versa.*

Proofs for Prop. 1 and Prop. 2 are in the supplementary. The ordinalities here rely on  $\mathcal{H}$ , the heat from absorbed visible light. Next, we incorporate invisible light and relate  $\mathcal{H}$  to thermal image intensity,  $I_t$ .

### 3.2. Visible and Invisible Illumination

Common light sources such as sunlight and incandescent lamps emit significant invisible radiation (e.g., infrared). While the visible camera captures only reflected light within its spectral response, heat generation arises from absorbed energy across all wavelengths. Thus, the equation for the heat source intensity has an additional term as follows:

$$\mathcal{H} = (1 - \rho_v)\eta + (1 - \rho_i)\frac{l_i}{l_v}\eta, \quad (7)$$

where  $\rho_i$  is the average albedo in the invisible band,  $l_i/l_v$  is the ratio of light intensity in the invisible and visible spectra.

While albedo variations are prominent in the visible spectrum, their counterparts in the infrared are much smaller [9]. Thus, we assume that  $\rho_i$  is locally constant within a region, allowing (7) to be approximated as:

$$\mathcal{H} = (\beta - \rho_v)\eta, \quad \text{s.t.} \quad \beta = 1 + (1 - \rho_i)l_i/l_v. \quad (8)$$

As  $\beta$  is locally constant, (5b) still holds as  $\nabla\mathcal{H}$  is invariant to a constant offset in  $\mathcal{H}$ . Also, as  $\beta > 1$ , Prop. 1 and Prop. 2 holds whenever  $\beta$  is same for the two points.

### 3.3. Relating heat intensity to a single thermal image

The heat transport equation at a surface point is:

$$C_h \frac{\partial T}{\partial t} = \mathcal{H} + h_c(T_a - T) + 4\epsilon\sigma T_s^3(T_s - T) + \kappa\Delta T, \quad (9)$$

where  $C_h$  is the heat capacity,  $T$  the surface temperature,  $t$  time,  $h_c$  the convection coefficient,  $T_a$  the air temperature,  $\epsilon$  the surface emissivity,  $\sigma$  the Stefan-Boltzmann constant,  $T_s$  the surrounding temperature,  $\kappa$  the thermal conductivity, and  $\Delta$  denotes the Laplacian operator along the surface. A static scene under constant lighting reaches thermal equilibrium when the left side of (9) is zero, giving

$$\mathcal{H} = (h_c + 4\epsilon\sigma T_s^3)T - \kappa\Delta T - (h_c T_a + 4\epsilon\sigma T_s^4). \quad (10)$$

The image intensity measurement  $I_t$  made by a thermal camera is related to the temperature  $T$  as follows:

$$I_t = \epsilon U(T) + (1 - \epsilon)U(T_s), \quad (11)$$

where  $U$  denotes the thermal camera's response function. Linearizing  $U$  as  $U(T) = p_1 T + p_2$  in (11), we get

$$T = a_1 I_t - a_2 \quad \text{s.t.} \quad a_1 = \frac{1}{\epsilon p_1}, \quad a_2 = \frac{p_2 + p_1 T_s(1 - \epsilon)}{\epsilon p_1}. \quad (12)$$

Substituting (12) in (10), we get

$$\mathcal{H} = c_1 I_t - c_2 \Delta I_t - c_3, \quad (13)$$

where  $c_1 = \frac{h_c + 4\epsilon\sigma T_s^3}{\epsilon p_1}$ ,  $c_2 = \frac{\kappa}{\epsilon p_1}$ , and  $c_3 = (h_c + 4\epsilon\sigma T_s^3) \left( \frac{p_2 + p_1 T_s(1 - \epsilon)}{\epsilon p_1} \right) + (h_c T_a + 4\epsilon\sigma T_s^4)$ .

The thermal properties such as  $\epsilon$ , and  $\kappa$  have small variations irrespective of the variation in albedo [40]. The environmental variables such as  $h_c$ ,  $T_a$ , and  $T_s$  are also similar. Therefore,  $c_1$ ,  $c_2$  and  $c_3$  are similar within a region. Also, thermal conductivity of many common materials, excluding metals, is low. Likewise, the Laplacian of a temperature field at steady state has a much smaller magnitude than absolute temperatures [40]. Therefore, we ignore the conduction term. Then, as  $c_1 > 0$ , the ordinal relationships between  $\mathcal{H}$  at two points is the same as that of  $I_t$ .

**Proposition 3.** *In local regions,  $c_1$ ,  $c_2$  and  $c_3$  are constant so that for any two pixels  $x_i, x_j$ , if  $\mathcal{H}(x_i)$  is less (or more) than  $\mathcal{H}(x_j)$ , then  $I_t(x_i)$  is also less (or more) than  $I_t(x_j)$ .*

### 3.4. Ordinality of Albedo and Shading

Using Prop. 3, we can extend the results from Eq. 5b to use thermal image intensities, as summarized below:

$$\text{Albedo Edge}(\nabla\eta = 0): \text{sign}(\nabla I_v) = -\text{sign}(\nabla I_t), \quad (14a)$$

$$\text{Shading Edge}(\nabla\rho = 0): \text{sign}(\nabla I_v) = \text{sign}(\nabla I_t). \quad (14b)$$

Similarly, we extend Prop. 1 and Prop. 2 to thermal image intensities, yielding the following ordinal relationships:

$$I_v(x_i) > I_v(x_j), I_t(x_i) > I_t(x_j) \Rightarrow \eta(x_i) > \eta(x_j), \quad (15a)$$

$$I_v(x_i) < I_v(x_j), I_t(x_i) < I_t(x_j) \Rightarrow \eta(x_i) < \eta(x_j), \quad (15b)$$

$$I_v(x_i) > I_v(x_j), I_t(x_i) < I_t(x_j) \Rightarrow \rho(x_i) > \rho(x_j), \quad (15c)$$

$$I_v(x_i) < I_v(x_j), I_t(x_i) > I_t(x_j) \Rightarrow \rho(x_i) < \rho(x_j). \quad (15d)$$

### 3.5. Expert Validation on Ordinalities

We validated the accuracy and robustness of our theory of ordinalities on a wide range of real-world materials and scenes by comparing against domain expert labeling.

**Patch Ordinality on Various Materials.** The first evaluation included 20 patches from CURET dataset [10] and common objects (painted aluminum, plastic, wood, silk, leather, cloth, plaster, etc.). These patches were placed in different orientations under artificial and natural lighting. Experts confidently labeled 865 ordinalities across patches. Our prediction matched the expert labels with 98.59% accuracy in sunlight (albedo: 99.37%, shading: 97.01%) and 96.82% under white-LED (albedo: 94.62%, shading: 100%).

**Point-Pair Ordinality on Diverse Scenes.** We further evaluated on 100 real-world scenes in VT-Intrinsic dataset (Sec. 5), spanning materials such as stone, concrete, grass, vegetation, painted metal, plastic, and wood. Experts labeled the ordinalities in albedo or shading of 20 randomly sampled point pairs per image using the visible image as reference. Pairs with small intensity differences were excluded to avoid ambiguity. Experts confidently labeled 1,063 pairs and found 937 unclear. Ignoring the latter, our theory achieved 98.95% overall accuracy (albedo: 96.96%, shading: 99.62%), confirming the reliability of thermal-guided ordinal cues. *More details are in the supplementary.*

## 4. Method

Using the ordinalities as loss functions, we optimize the albedo and shading from a visible-thermal image pair. Let  $I_v$  be a  $k$ -channel visible image and  $I_t$  be the corresponding aligned thermal image. Let  $\hat{\rho}$  and  $\hat{\eta}$  be an estimate of the  $k$ -channel albedo and grayscale shading. Let  $\bar{I}_v$  and  $\bar{\rho}$  be the grayscale image and albedo estimate, respectively.

### 4.1. Local (Edge) Loss

Using Eq. 14, we label edges (A for albedo, S for shading) based on their local visible-thermal gradients (Fig. 2):

$$\mathcal{C}(x) = \begin{cases} \text{A} & |\nabla \bar{I}_v| > \epsilon_m, \left| \frac{\nabla \bar{I}_v \nabla \bar{I}_t}{\|\nabla \bar{I}_v\| \|\nabla \bar{I}_t\|} \right| > \epsilon_p, \\ \text{S} & |\nabla \bar{I}_v| > \epsilon_m, \left| \frac{\nabla \bar{I}_v \nabla \bar{I}_t}{\|\nabla \bar{I}_v\| \|\nabla \bar{I}_t\|} \right| < \epsilon_p, \end{cases} \quad (16)$$



where  $\epsilon_m$  suppresses textureless regions and  $\epsilon_p$  thresholds the cosine similarity between visible and thermal gradients.

Before computing  $\nabla I_t$ , we apply Gaussian smoothing to reduce noise while maintaining gradient consistency.

With the class labels above, we formulate an edge loss that penalizes albedo gradients at shading-dominant pixels and vice versa, where  $\Omega$  denotes all image pixels:

$$\mathcal{L}_{\text{edge}}(\bar{\rho}, \hat{\eta}, \mathcal{C}) = \frac{1}{|\Omega|} \left[ \sum_{\mathcal{C}(x)=S} \|\nabla \bar{\rho}(x)\|^2 + \sum_{\mathcal{C}(x)=A} \|\nabla \hat{\eta}(x)\|^2 \right]. \quad (17)$$

## 4.2. Non-Local (Point-Pair) Loss

During optimization, we use Poisson disk sampling [5] to generate random point pairs across the image. Using Eq. 15, each pair  $(x_i, x_j)$  is assigned a class label based on their normalized intensity differences  $\delta I_v$  and  $\delta I_t$ :

$$\mathcal{P}(x_i, x_j) = \begin{cases} S_+ & \delta I_v > \epsilon_d, \delta I_t > \epsilon_d, \\ S_- & \delta I_v < -\epsilon_d, \delta I_t < -\epsilon_d, \\ A_+ & \delta I_v > \epsilon_d, \delta I_t < -\epsilon_d, \\ A_- & \delta I_v < -\epsilon_d, \delta I_t > \epsilon_d, \end{cases} \quad (18)$$

where  $\delta I_x = \frac{I_x(x_i) - I_x(x_j)}{Z_x}$  with normalization  $Z_x$  so that threshold  $\epsilon_d$  is relative. The ordinal loss is a hinge-based formulation that enforces separation beyond a margin  $\epsilon_m$ :

$$\mathcal{L}_{\text{ord}} = \frac{1}{|\mathcal{P}|} \sum_{(x_i, x_j)} \begin{cases} \max(\hat{\eta}_j - \hat{\eta}_i + \epsilon_m, 0), & \mathcal{P}(x_i, x_j) = S_+, \\ \max(\hat{\eta}_i - \hat{\eta}_j + \epsilon_m, 0), & \mathcal{P}(x_i, x_j) = S_-, \\ \max(\bar{\rho}_j - \bar{\rho}_i + \epsilon_m, 0), & \mathcal{P}(x_i, x_j) = A_+, \\ \max(\bar{\rho}_i - \bar{\rho}_j + \epsilon_m, 0), & \mathcal{P}(x_i, x_j) = A_-. \end{cases} \quad (19)$$

## 4.3. Regularization using Deep Image Prior

In complex real scenes, thermal noise can corrupt subtle gradients, and ordinal constraints alone cannot fully determine absolute albedo or shading values—they only restrict the solution space. Therefore, we adopt a variant of the Deep Image Prior [39] to parameterize albedo and shading, leveraging the inherent architectural prior in a randomly initialized network for regularization.

We employ a Double-DIP (DDIP) architecture [16] with two networks  $\mathcal{N}(z_A, \Theta_A)$ ,  $\mathcal{N}(z_S, \Theta_S)$  to parameterize albedo and shading, respectively. Each uses a convolutional encoder-decoder with skip connections [39].  $\Theta_A, \Theta_S$  are randomly initialized model weights and  $z_A, z_S$  are randomly sampled input noise vectors. The albedo network outputs a  $k$ -channel image bounded to  $[0, 1]^k$  via a sigmoid activation, while the shading network predicts a single channel constrained by a non-negativity penalty. We freeze  $z_A$  and  $z_S$  while only optimizing for  $\Theta_A$  and  $\Theta_S$ .

## 4.4. Optimization

Our complete objective function is as follows.

$$\mathcal{L}(\hat{\rho}, \hat{\eta}, I_v, I_t) = \|\hat{\rho} \cdot \hat{\eta} - I_v\|_2 + \lambda_1 \mathcal{L}_{\text{edge}}(\bar{\rho}, \hat{\eta}, \mathcal{C}(\bar{I}_v, I_t)) + \lambda_2 \mathcal{L}_{\text{ord}}(\bar{\rho}, \hat{\eta}, \mathcal{P}(\bar{I}_v, I_t)), \quad (20)$$

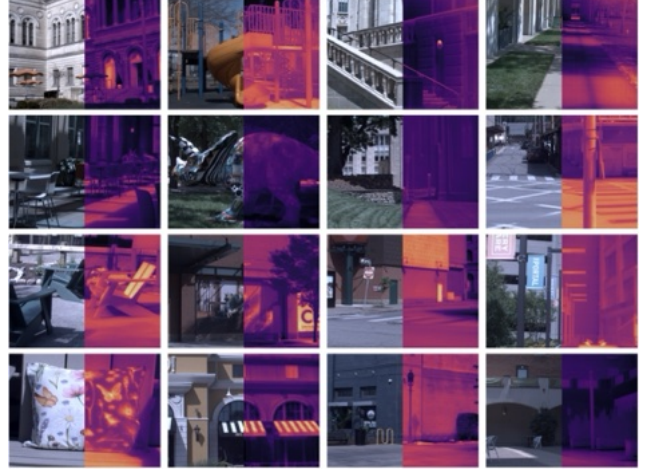


Figure 3. Examples from the visible-thermal image pairs in the VT-Intrinsic dataset, covering diverse scenes including parks, schools, cathedrals, plazas, museums, and various urban streets.

where  $\lambda_1, \lambda_2 > 0$  are the respective loss weights. The thermal image is used only for edge or point pair losses, which operate on the mean albedo. The reconstruction loss is defined on the  $k$ -channel image.

## 5. VT-Intrinsic Dataset

Existing IID datasets lack thermal modalities, while current visible-thermal datasets (e.g., captured from vehicles or drones) focus on dynamic objects (people, cars) or non-light-absorption based heat sources (engines, people) that are out of scope for this work. So, we collected 600 visible-thermal image pairs (Fig. 3) across diverse stationary scenes under varying illumination to validate our method.

**Imaging System:** We co-locate a FLIR Boson thermal camera ( $512 \times 640$  resolution,  $24^\circ$  HFOV,  $\leq 50\text{mK}$  NEDT) with an IDS UI-3130 color camera ( $600 \times 800$  resolution,  $27^\circ$  HFOV) using a gold dichroic mirror (BSP-DI-25-2). For distant outdoor scenes, the cameras are placed side by side and aligned via homography.

**Data Acquisition and Preprocessing:** We captured 20 exposure-bracketed color images with geometrically spaced exposure times and merged them into a linear HDR image [13] after edge-aware demosaicing in OpenCV. Five frames were averaged to suppress sensor noise. The visible HDR and thermal images were aligned via homography.

Our dataset contributes to the research community in two key aspects. First, it provides a large collection of high-quality real-world outdoor images with diverse albedo-shading combinations, whereas prior datasets are predominantly indoor or synthetic. Second, it offers abundant pseudo-ground-truth ordinalities of albedo and shading, facilitating model training and evaluation. As shown in Sec. 3.5, the thermal image produces reliable ordinalities across *arbitrary pixel pairs*—previously only available in limited form due to costly human labeling (IIW [5]).

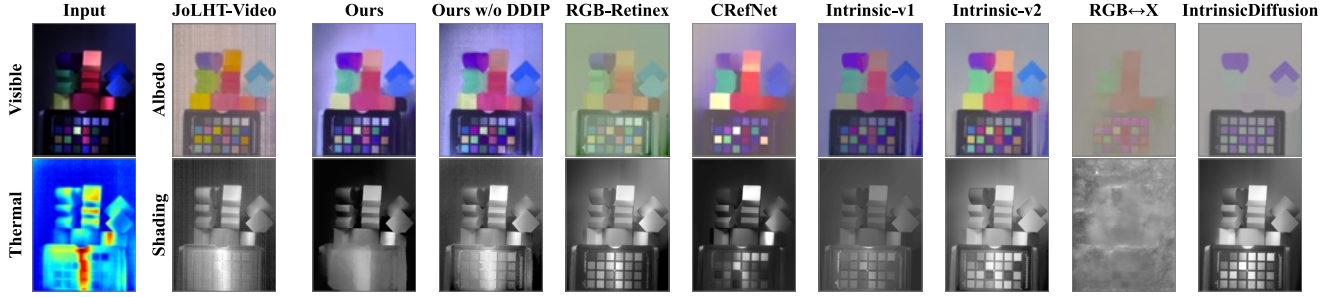


Figure 4. Results on a color-chart scene in JoLHT-Video dataset. Our method recovers the smooth line-light shading across the color chart.

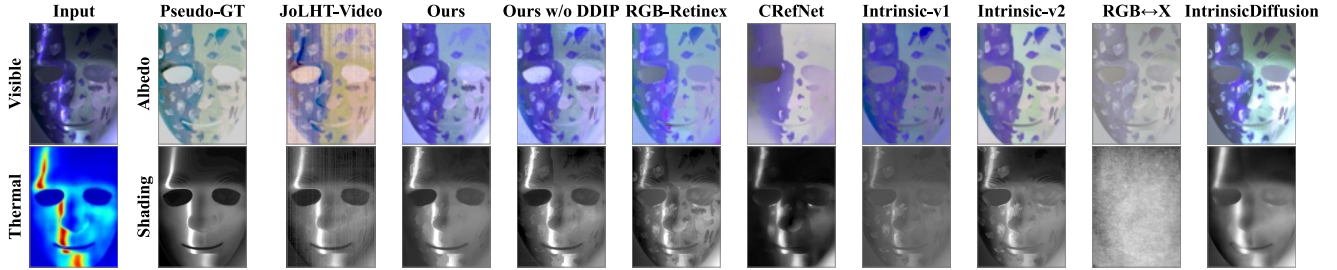


Figure 5. Results on *Painted-Mask* scene in JoLHT-Video dataset. Baselines show albedo texture in shading or highlight artifacts in albedo.

## 6. Experiments

**Datasets:** As typical IID datasets lack associated thermal images, we construct the VT-Intrinsic dataset for qualitative evaluation. Obtaining ground truth albedo and shading for real-world scenes is impractical. Therefore, for quantitative evaluation, we collected images of a color chart under different illuminations - white LED light, incandescent bulb and sunlight. We also evaluate on the dataset from JoLHT-Video [33], which contains four scenes of a color chart under varied illuminations and a *Painted-Mask* scene. Finally, we evaluate on the MIT-Intrinsics [19] dataset by simulating an ideal thermal image using their pseudo-ground truth.

**Metrics:** We use the scale-invariant Mean Square Error (si-MSE) to evaluate albedo and shading quantitatively.

**Baselines:** We compare with state-of-the-art methods in three categories. *Learning-based:* Diffusion-based IntrinsicDiffusion [29] and RGB↔X [42], CNN-based Intrinsic-v1 [6] and Intrinsic-v2 [7], and Transformer-based CRefNet [30]. *Physics-based:* NIR-Priors [8], requiring a paired NIR image, and JoLHT-Video [33], demanding transient thermal video under controlled illumination. *Optimization-based:* RGB-Retinex [20] and Opt-LocalSmooth [36]. IntrinsicDiffusion, RGB↔X, and Intrinsic-v2 output colorful shading, while others grayscale.

### 6.1. Quantitative Evaluation

In this section, we present quantitative comparisons on the simulated MIT-Intrinsics dataset, color charts under different illumination, and JoLHT-Video data [33], including an ablation on the loss terms and Double-DIP parameterization. The optimization generally converges in 5000 iterations with Double-DIP parameterization and 500 without, averaging approximately 1 min and 5 s per pair on a

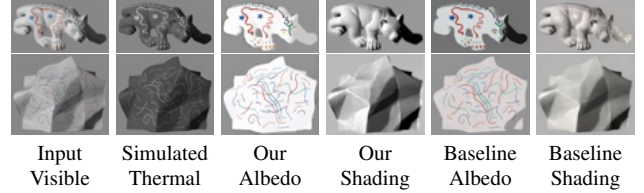


Figure 6. Qualitative comparison with the best baseline on MIT Intrinsic dataset [19], IntrinsicDiffusion [29]. Our method excels without learning priors by leveraging the simulated thermal image.

GeForce RTX 4090 GPU with parallelization. In challenging cases, additional iterations offer modest gains.

#### 6.1.1. Simulated MIT Intrinsics Dataset

The effectiveness of our method depends on two orthogonal factors: (1) the correctness of albedo-shading ordinalities derived from visible-thermal pairs, determined by imaging quality and the robustness of our theory to variations in physical properties, and (2) the informativeness of such ordinalities for intrinsic decomposition. With (1) validated in Sec. 3.5, we isolate (2) by generating ideal absorbed-light images as thermal input using pseudo ground truth from the MIT Intrinsics dataset [19] via Eq. 2. Tab. 1 shows that a single ideal thermal image achieves the lowest mean si-MSE in 20 cases, surpassing learned priors and heuristics.

#### 6.1.2. Color Chart under Different Illuminations

We imaged a color chart under white LED, incandescent and sunlight. Tab. 1 shows our method outperforming baselines under all illuminations. Incandescent and sunlight experiments demonstrate our robustness to albedo variations even in the invisible band that influence absorbed light. In contrast, physics-based baselines have limited applicability: JoLHT-Video assumes no invisible lighting component, and NIR-Priors requires NIR emission absent in white LEDs.



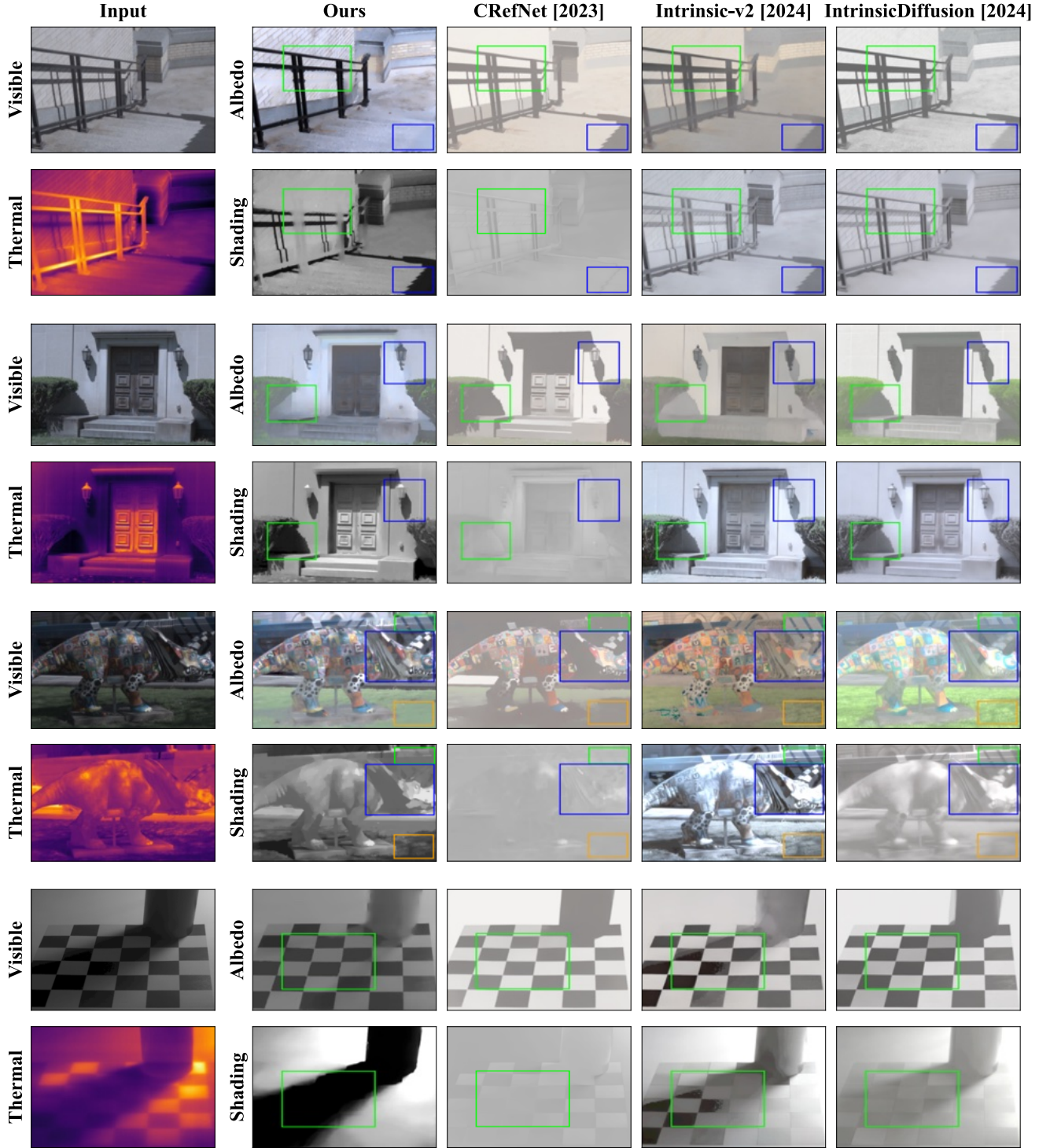


Figure 7. **Qualitative comparisons to state-of-the-art baselines.** The first two scenes show how our method removes cast shadows from albedo (e.g., shadow of handrail in case 1, lanterns in case 2). The next three demonstrate our ability to eliminate albedo texture from shading (e.g., rhino statue texture in case 3, checkerboard pattern in case 4). But baselines struggle with these challenges, despite their advantage of pre-training on large datasets, whereas our approach relies solely on physics-based information in a single thermal image. Baselines often over-smooth albedo and shading (e.g., smooth albedo on detailed ground and walls, flat shading on grass) due to reliance on priors. Diffusion-based baselines can offer appealing visual quality but sacrifice faithfulness (e.g. hallucinated albedo texture on the rhino statue in case 3). Images are tonemapped for visualization. Key differences are highlighted in bounding boxes. *More examples and baselines appear in the supplementary.*

Table 1. Results of si-MSE ( $\downarrow$ ) reported at  $10^{-2}$  across datasets (Sec. 6.1.3, Sec. 6.1.2, Sec. 6.1.1). **Best** and second highlighted. Our method surpasses all learning-based approaches despite using no learned priors and achieves performance comparable to JoLHT-Video, which demands transient thermal video under controlled illumination. N/A indicates unavailable data, and  $\times$  denotes non-applicability.

Method	MIT Intrinsic Dataset		Color Chart w/ Different Illumination			JoLHT-Video Dataset		
	Average	Average	White LED	Incandescent	Sunlight	Painted Mask		Color Charts
			Albedo	Albedo	Albedo	Albedo	Shading	Albedo
• Optimization-based								
♦ Learning-based								
★ Physics-based (w/ auxiliary sensor)								
• RGB-Retinex [20] (TPAMI'06)	15	9.1	2.42	2.33	2.73	25	0.30	3.4
• Opt-LocalSmooth [36] (CVPR'11)	5.7	2.7	2.41	4.21	2.04	45	0.35	7.1
♦ IntrinsicDiffusion [29] (SIGGRAPH'24)	3.3	<u>1.2</u>	4.12	3.33	4.85	37	0.25	2.9
♦ RGB $\leftrightarrow$ X [42] (SIGGRAPH'24)	<u>3.1</u>	2.4	4.07	5.31	4.59	30	0.37	2.8
♦ Intrinsic-v2 [7] (ToG'24)	5.6	1.5	<u>1.25</u>	4.36	4.17	27	0.17	2.8
♦ Intrinsic-v1 [6] (ToG'23)	5.0	3.2	1.55	2.72	4.97	30	0.21	3.8
♦ CRefNet [30] (TVCG'23)	4.9	2.6	1.79	<u>2.29</u>	<u>1.98</u>	38	0.23	8.8
★ NIR-Priors [8] (ICCV'19)	N/A	N/A	$\times$	2.46	2.08	N/A	N/A	N/A
★ JoLHT-Video [33] (CVPR'24)	N/A	N/A	N/A	$\times$	$\times$	<b>8.4</b>	<b>0.05</b>	<b>2.0</b>
★ Ours	<b>1.9</b>	<b>0.5</b>	<b>0.37</b>	<b>1.06</b>	<b>1.19</b>	<u>11</u>	<u>0.10</u>	<u>2.7</u>

### 6.1.3. Using JoLHT-Video Data

The dataset includes four color-chart scenes and a *Painted-Mask* scene with pseudo ground-truth obtained following [19], which are considerably more challenging due to the strong lighting variations from line light (e.g. Fig. 4, Fig. 5). As shown in Tab. 1, our method consistently outperforms all learning-based baselines despite not relying on pre-trained priors, and achieves performance comparable to JoLHT-Video [33], which operates under stricter conditions requiring transient thermal video under controlled lighting.

### 6.1.4. Ablation on Loss Terms and DDIP

We ablated the loss functions and Double-DIP parameterization using pseudo ground truth from the *Painted Mask* scene. Tab. 2 shows that combining ordinal, edge, and reconstruction losses with Double-DIP yields the best result.

Table 2. Ablation study on loss terms and Double-DIP parameterization. We report the si-MSE for the *Painted Mask* scene.

$\mathcal{L}_{\text{recon}}$	$\mathcal{L}_{\text{edge}}$	$\mathcal{L}_{\text{ord}}$	DDIP	Albedo $\downarrow$	Shading $\downarrow$
✓	✓	✓	✓	$1.1 \times 10^{-1}$	$9.7 \times 10^{-4}$
✓	✓	✓	$\times$	$1.6 \times 10^{-1}$	$32 \times 10^{-4}$
✓	✓	$\times$	✓	$2.2 \times 10^{-1}$	$18 \times 10^{-4}$
✓	$\times$	✓	✓	$2.0 \times 10^{-1}$	$13 \times 10^{-4}$
$\times$	✓	✓	✓	$4.0 \times 10^{-1}$	$79 \times 10^{-4}$
✓	$\times$	$\times$	✓	$3.3 \times 10^{-1}$	$22 \times 10^{-4}$

## 6.2. Qualitative Evaluation

Fig. 7 presents comparisons with state-of-the-art baselines across various scenes. The first two cases demonstrate our ability to remove cast shadows from albedo (e.g., handrail and lantern shadows), while the next two highlight disentangling albedo texture from shading (e.g., rhino statue texture and checkerboard pattern). The final example is an homage to the classic Adelson’s Checker-Shadow Illusion [1], where our method successfully separates the shadowed checker region from the cylinder shading.

Learning-based baselines often over-smooth albedo and shading due to strong statistical priors, producing flat grass shading or overly uniform wall colors. In contrast, our physics-based approach, guided solely by a single thermal image, better preserves details such as block-wise albedo variation, concrete texture, and natural shading gradients.

Fig. 4 and Fig. 5 show results on the JoLHT-Video dataset, where our method faithfully recovers smooth line-light shading without albedo leakage—comparable to JoLHT-Video—while relying only on a single thermal image. In contrast, baseline methods exhibit albedo leakage in shading or highlight artifacts in albedo.

*More cases and baselines are in the supplementary.*

## 7. Limitations and Conclusion

This work explores photometric cues encoded in a single auxiliary thermal image, and presents physics-based optimization for albedo-shading separation. We showed its effectiveness on real scenes with a wide range of materials and lighting conditions. However, diffuse reflection dominates in these materials — metals, transparent objects and mirrors violate the visible image formation model. Our model also assumes that the heat arises primarily from light absorption — heat generated otherwise internally (engines, humans) or externally (hot air blower or fire) is not modeled. Finally, we rely on inexpensive microbolometer thermal cameras whose quality is lower compared to visible cameras — low SNR due to insufficient heat generation (overcast skies, dynamic objects) can degrade performance. *Failure cases and an SNR analysis of lighting intensity versus performance are provided in the supplementary.* Despite these limitations, the strong improvements over all baselines demonstrate the potential to scale supervision for learning algorithms. We hope our work inspires further exploration of light-heat transport in vision and graphics.



## 8. Acknowledgements

This work was partly supported by NSF grants IIS210723, and NSF-NIFA AI Institute for Resilient Agriculture.

We are sincerely grateful to Akihiko Oharazawa for his help with expert annotation, and to Sriram Narayanan and Gaurav Parmar for their insightful discussions.

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# Physics-Based Decomposition of Reflectance and Shading using a Single Visible-Thermal Image Pair

## Supplementary Material

### 1. Proof for Propositions

**Proposition 1.** *Given two pixels with visible and heat intensities as in (6), if  $\mathcal{H}(x_i) > \mathcal{H}(x_j)$  and  $I_v(x_i) < I_v(x_j)$ , then  $\rho(x_i) < \rho(x_j)$ , and vice versa.*

*Proof.* Given

$$(1 - \rho(x_i))\eta(x_i) > (1 - \rho(x_j))\eta(x_j) \quad (21)$$

$$g\rho(x_i)\eta(x_i) < g\rho(x_j)\eta(x_j). \quad (22)$$

Dividing the first eq. by the second and noting that all terms are positive, we get

$$\frac{1 - \rho(x_i)}{g\rho(x_i)} > \frac{1 - \rho(x_j)}{g\rho(x_j)} \implies \rho(x_i) < \rho(x_j) \quad (23)$$

Proof for the complement is omitted for brevity.  $\square$

**Proposition 2.** *Given two pixels with visible and heat intensities as in (6), if  $I_v(x_i) < I_v(x_j)$  and  $\mathcal{H}(x_i) < \mathcal{H}(x_j)$ , then  $\eta(x_i) < \eta(x_j)$ , and vice versa.*

*Proof.* Since multiplying an inequality by a positive scalar and adding two inequalities of same order preserves the order, we have

$$\frac{I_v(x_i)}{g} + \mathcal{H}(x_i) < \frac{I_v(x_j)}{g} + \mathcal{H}(x_j). \quad (24)$$

From (1) and (2), note that  $\frac{I_v(x)}{g} + \mathcal{H}(x) = \eta(x)$ . Substituting in Eq. 24, we can see that

$$\eta(x_i) < \eta(x_j) \quad (25)$$

Proof for the complement is omitted for brevity.  $\square$

### 2. Ordinality Validation on Diverse Materials

To further examine how material properties affect the validity of our theory and assumptions, we created scenes with 20 common material samples from CURET dataset [10] and daily objects under sunlight and white-LED, and conducted expert validation on albedo-shading ordinalities. The detailed list of 20 materials used is shown in Tab. 3.

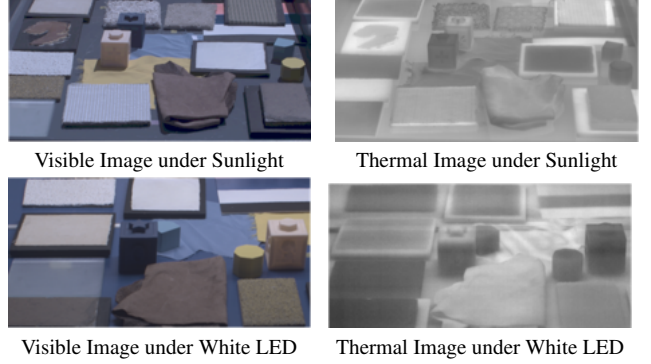


Figure 8. An example scene in expert validation on ordinalities across diverse materials (Sec. 3.5).

Table 3. The 20 materials used in ordinality validation.

1. Terrycloth	11. Orange peel
2. Plaster	12. Wooden block
3. Felt	13. Yellow silk
4. Cork	14. Blue silk
5. Frosted glass	15. Painted aluminum can
6. Sponge	16. Painted metal handcart
7. Carpet	17. Plastic board w/ black paint
8. White leather	18. Plastic board w/ white paint
9. Brick	19. Beige rubber block
10. Suede leather	20. Blue rubber block

### 3. Limitation and Failure Cases

The key limitations of our method arise when the relationship between the absorbed heat from light ( $S$ ) and the thermal image intensity ( $I_t$ ) is violated, which can be summarized by three categories: external heat generation, non-opaque surfaces, and low signal-to-noise ratio (SNR). Fig. 9 shows representative failure cases.

To investigate how thermal image SNR is influenced by low-light condition, we captured visible-thermal image pairs of a color chart under an incandescent light at different distance. We measured illuminance using a light meter and computed si-MSE on the albedo decomposed by our method. As shown in Fig. 10, si-MSE decreases with increasing illuminance, indicating improved thermal SNR and decomposition quality under higher illumination. For reference, direct sunlight reaches about 100,000 lux, while overcast daylight is around 6,000 lux [15].



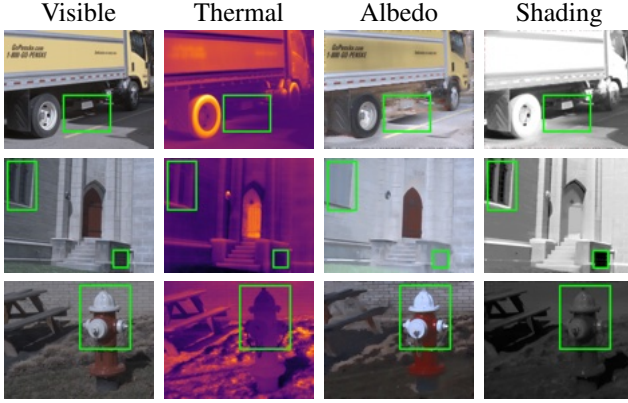


Figure 9. Corner cases: 1) The underside of a truck engine generates heat unrelated to light absorption, which elevates the thermal intensity of the road beneath it. 2) The cathedral windows are non-opaque, which violates the visible image formation model. 3) The metallic fire hydrant has low emissivity, resulting in poor thermal SNR, and exhibits specular highlights that challenge the common Lambertian assumption in IID.

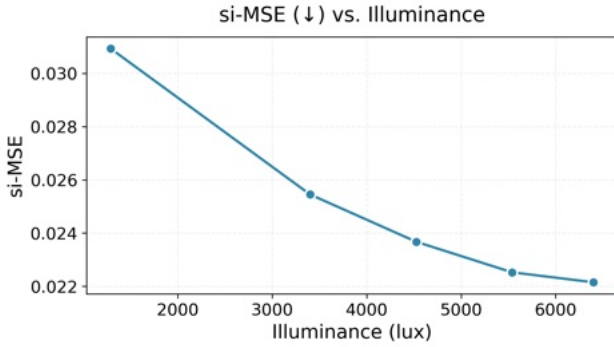


Figure 10. Effect of illuminance on albedo decomposition accuracy. The albedo si-MSE ( $\downarrow$ ) decreases as illuminance increases (incandescent bulb at varying distances), reflecting improved thermal SNR under stronger illumination. For reference, bright sunlight reaches 111,000 lux, while overcast daylight is typically 1,000–2,000 lux.

#### 4. Additional Qualitative Results

We provide additional qualitative results on VT-Intrinsic dataset in comparison with state-of-the-art baselines. Each case shows visible input with albedo estimations above and thermal with shading below. Images are tonemapped / colormapped for visualization.



Figure 11. Qualitative comparisons to state-of-the-art baselines. Visible input with albedo estimations are shown above and thermal with shading below.

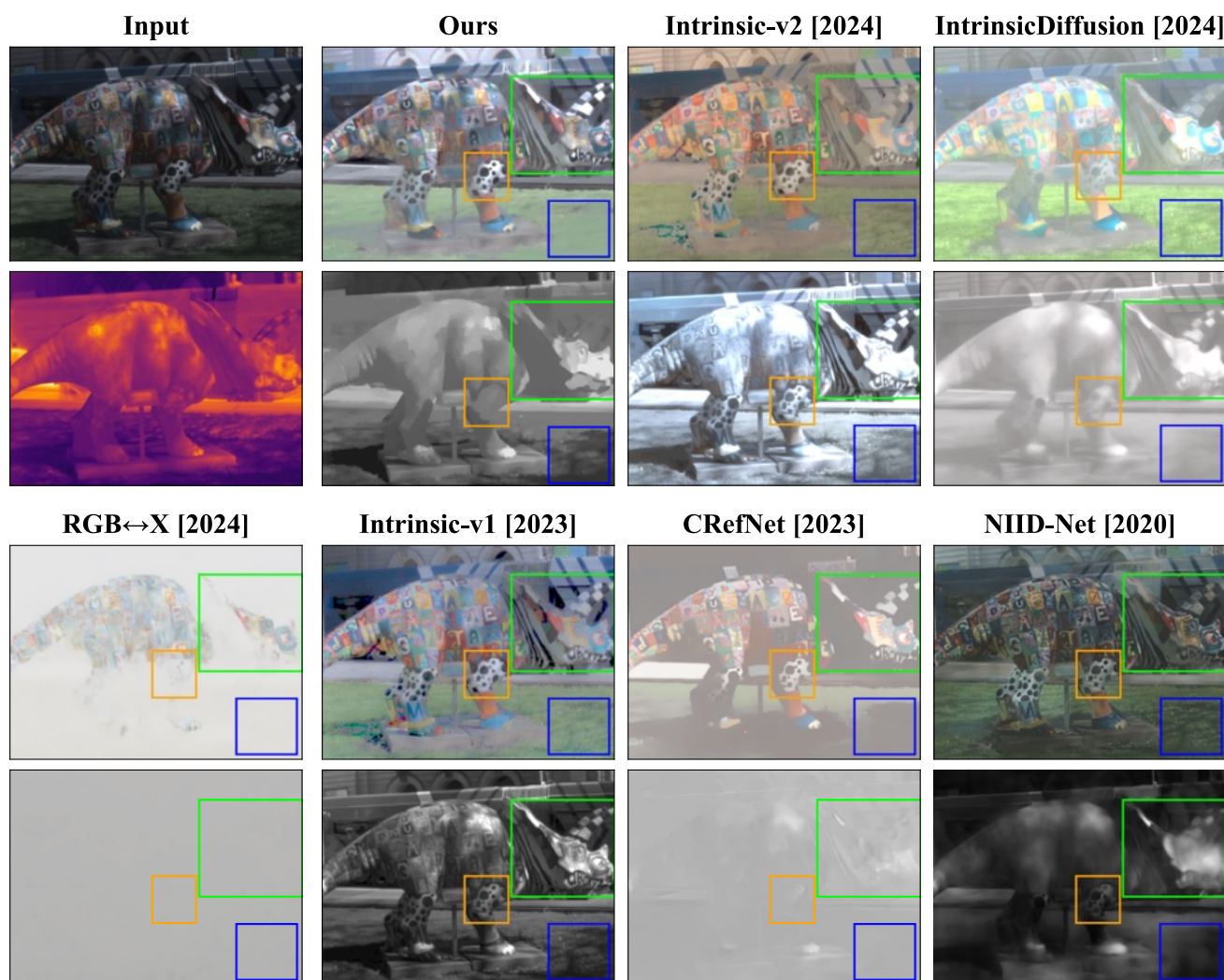


Figure 12. Qualitative comparisons to state-of-the-art baselines.



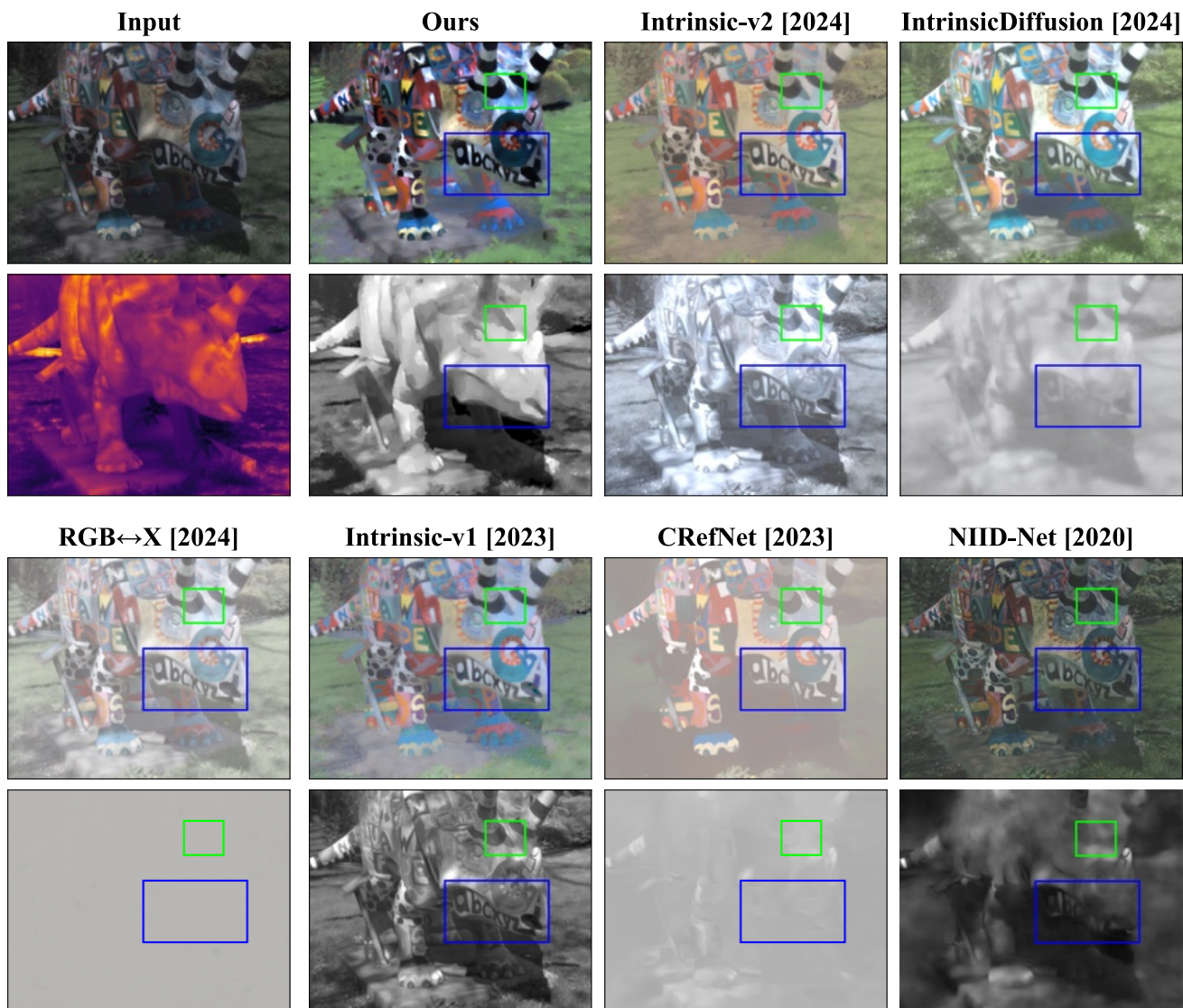


Figure 13. Qualitative comparisons to state-of-the-art baselines.

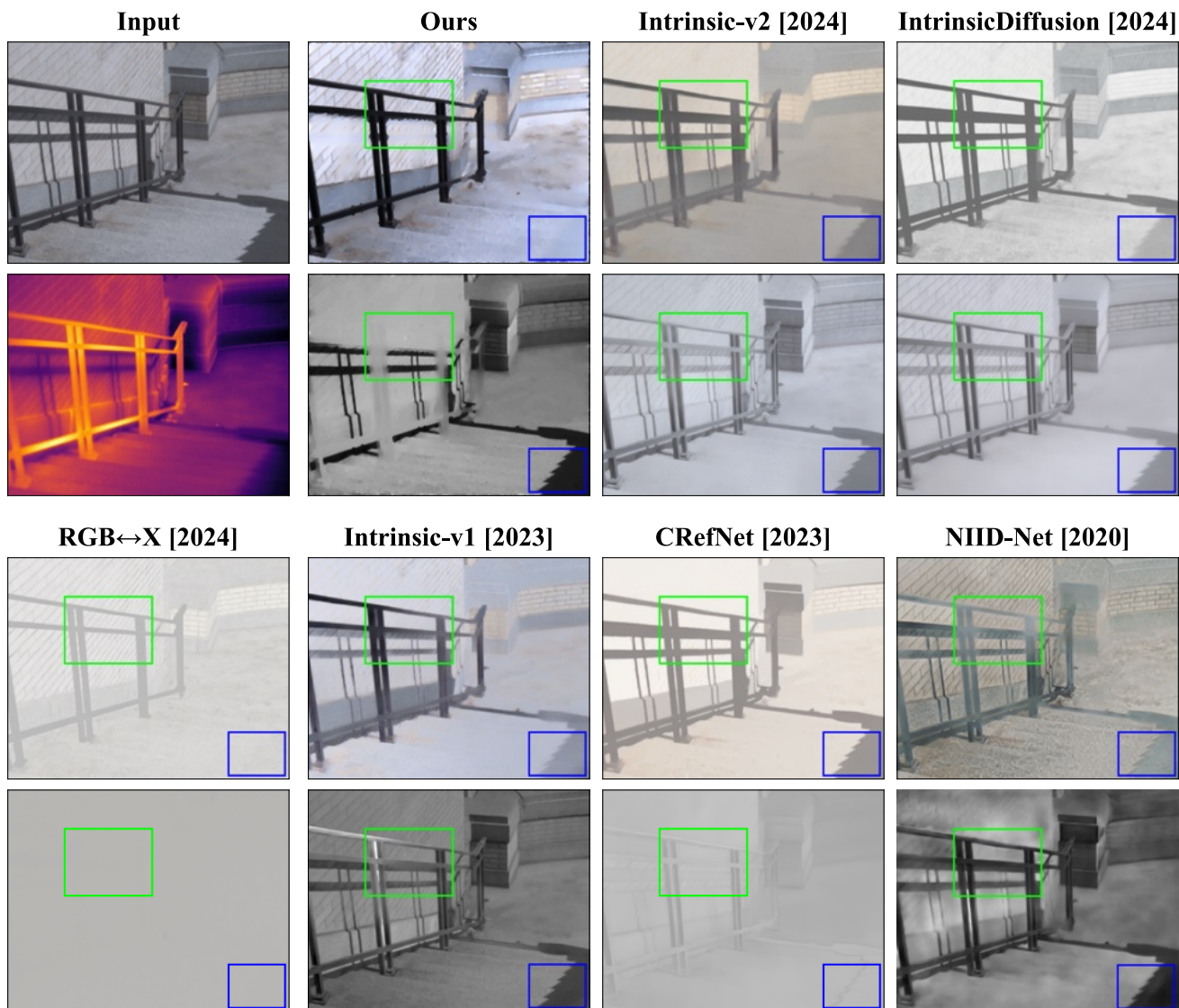


Figure 14. Qualitative comparisons to state-of-the-art baselines.

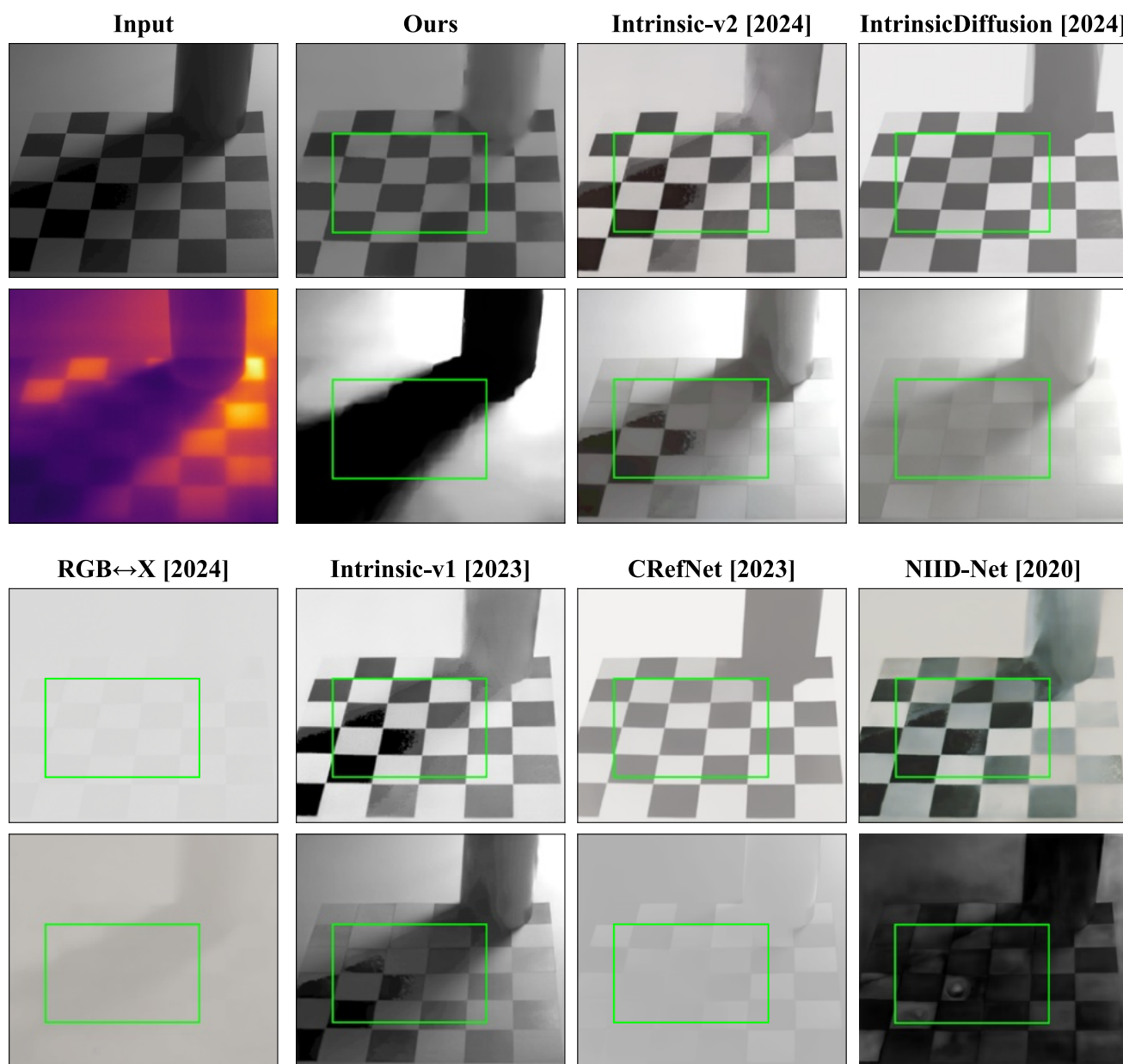


Figure 15. Qualitative comparisons to state-of-the-art baselines.



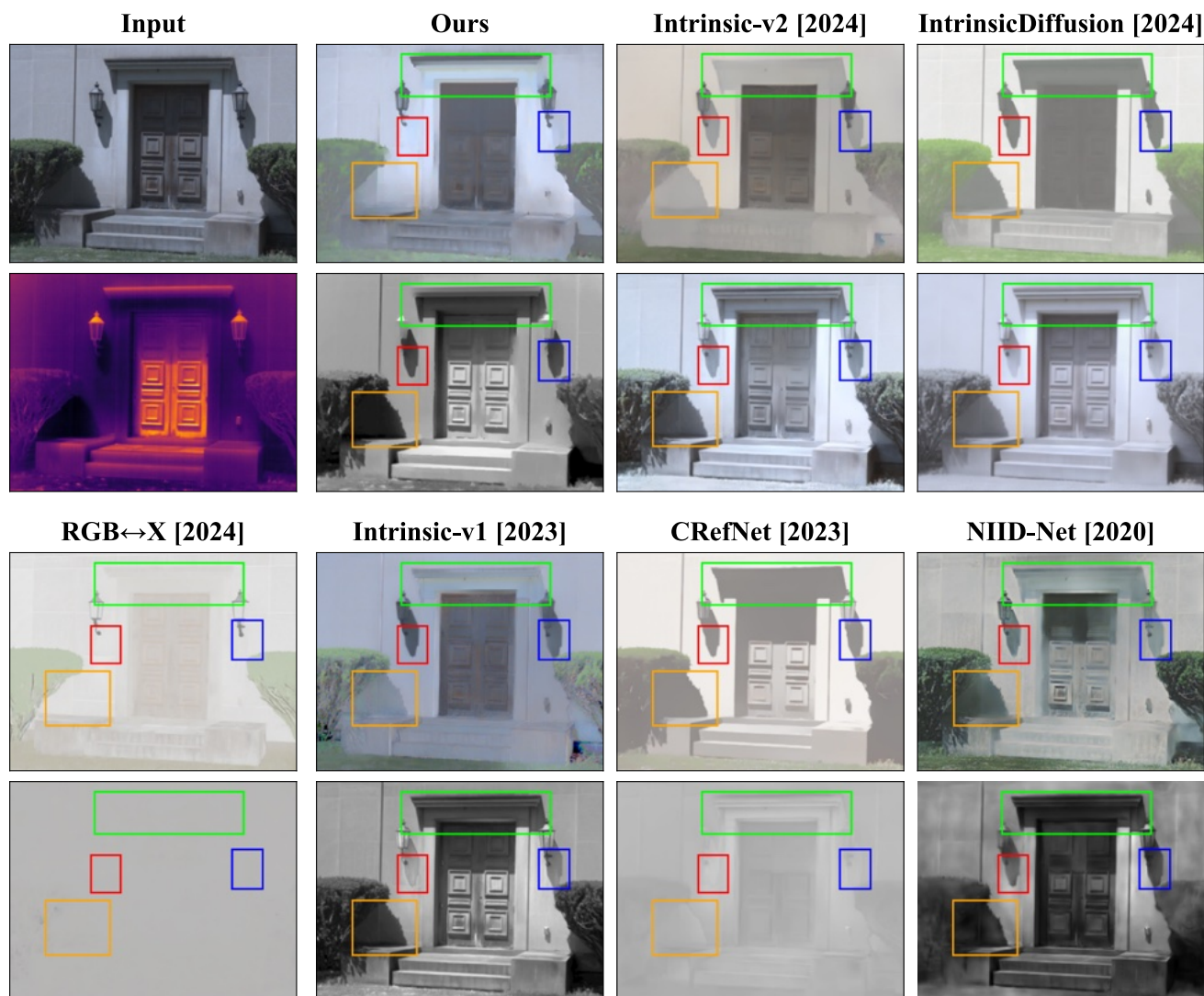


Figure 16. Qualitative comparisons to state-of-the-art baselines.

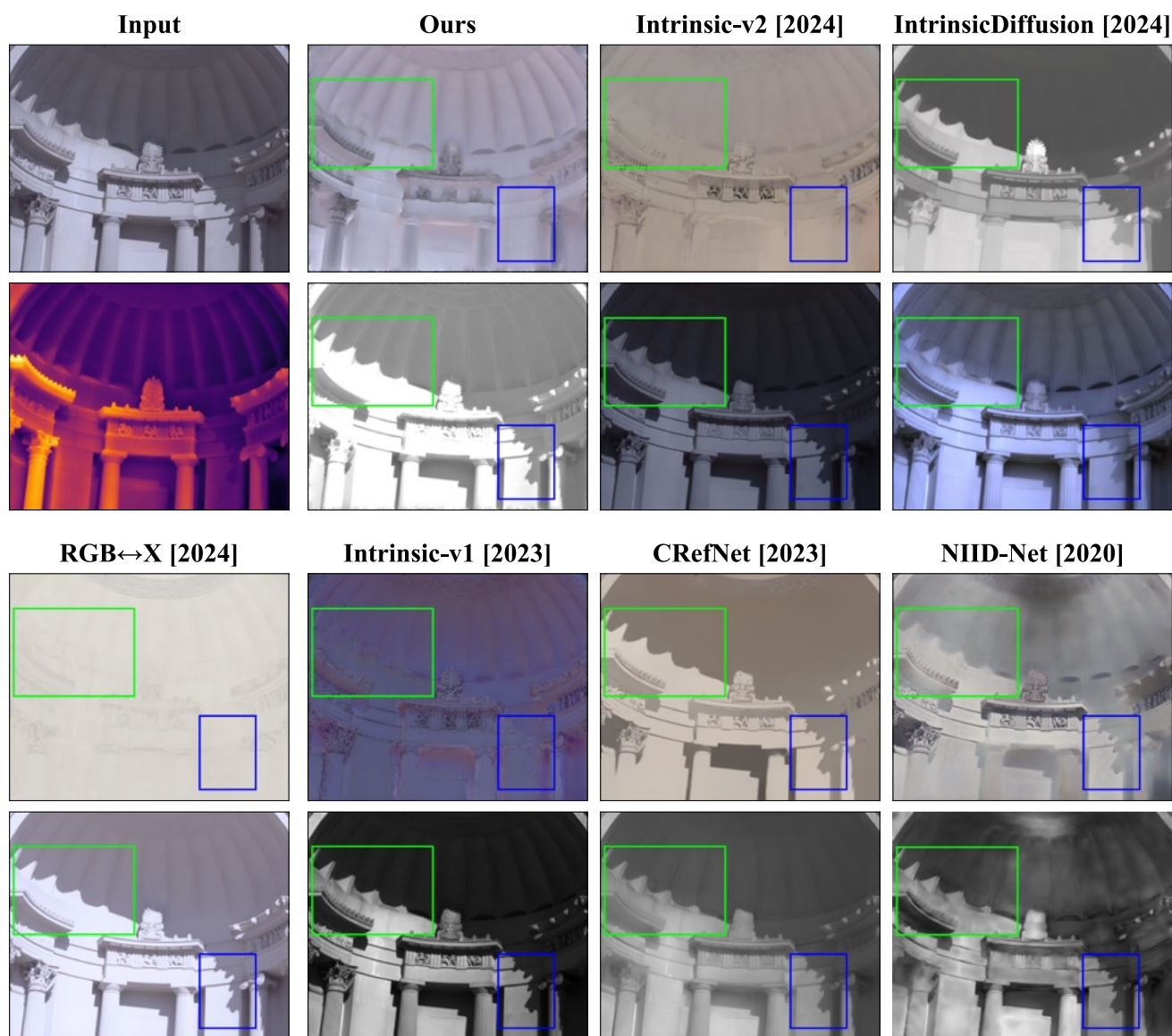


Figure 17. Qualitative comparisons to state-of-the-art baselines.



Figure 18. Qualitative comparisons to state-of-the-art baselines.



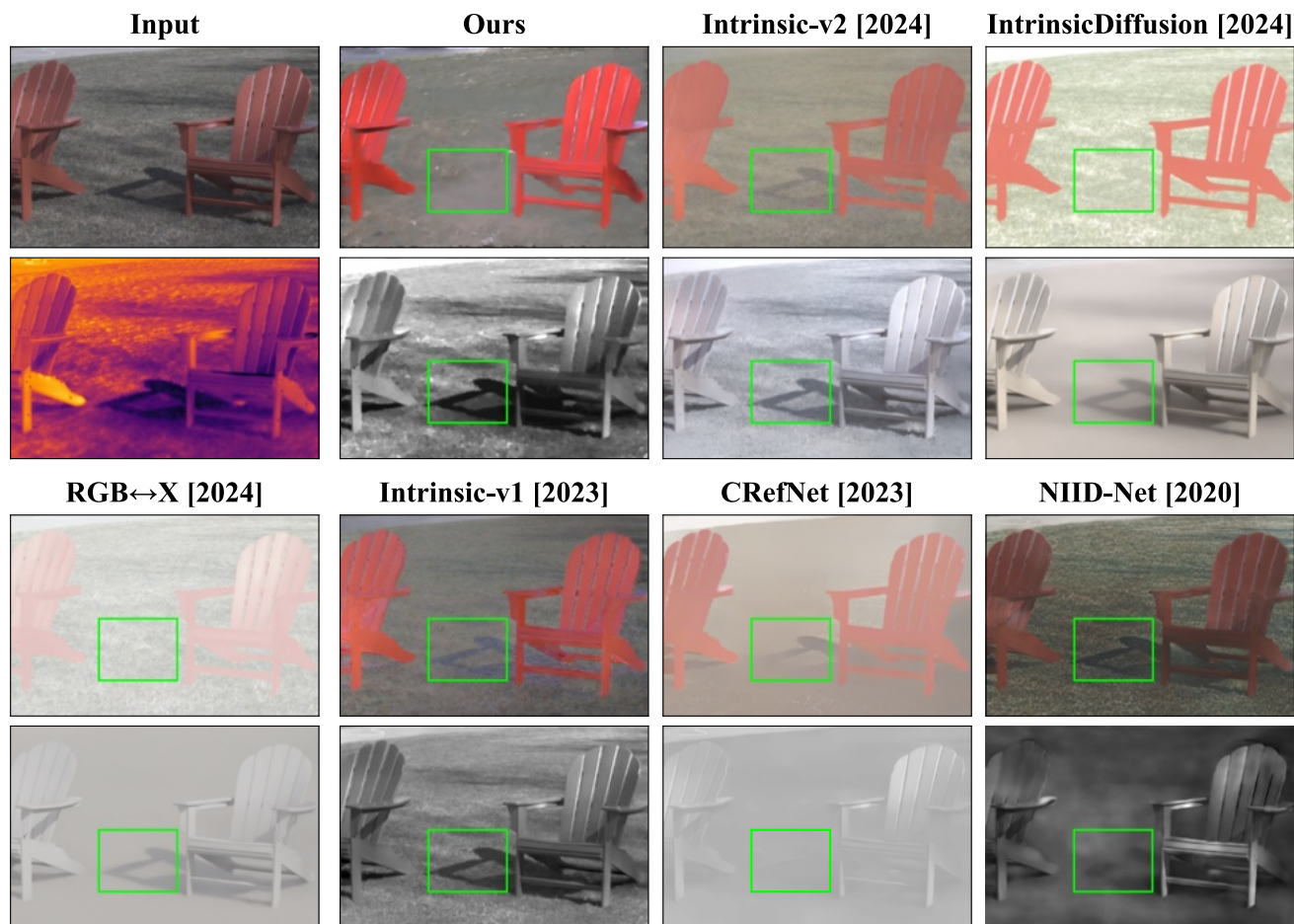


Figure 19. Qualitative comparisons to state-of-the-art baselines.

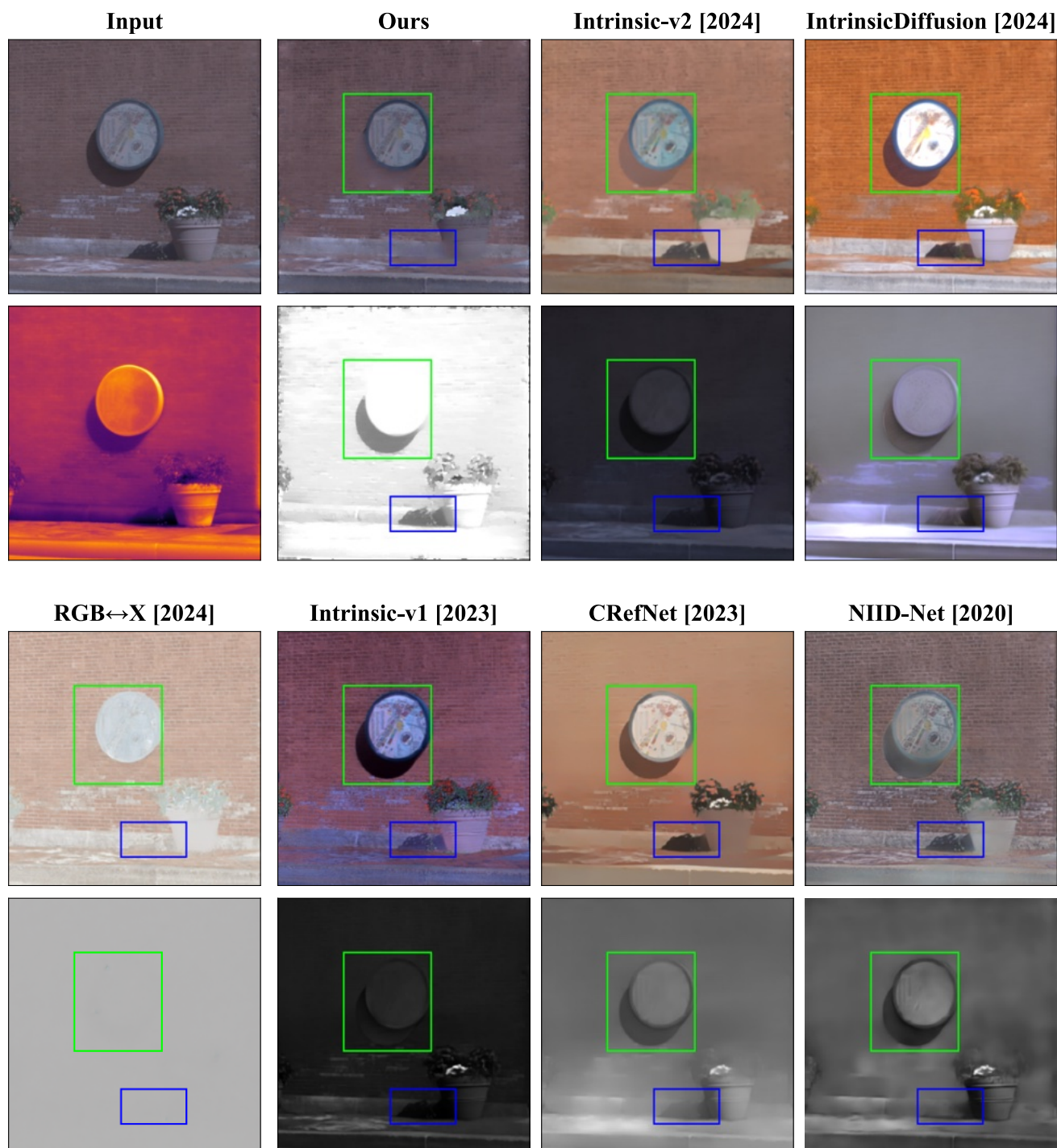


Figure 20. Qualitative comparisons to state-of-the-art baselines.

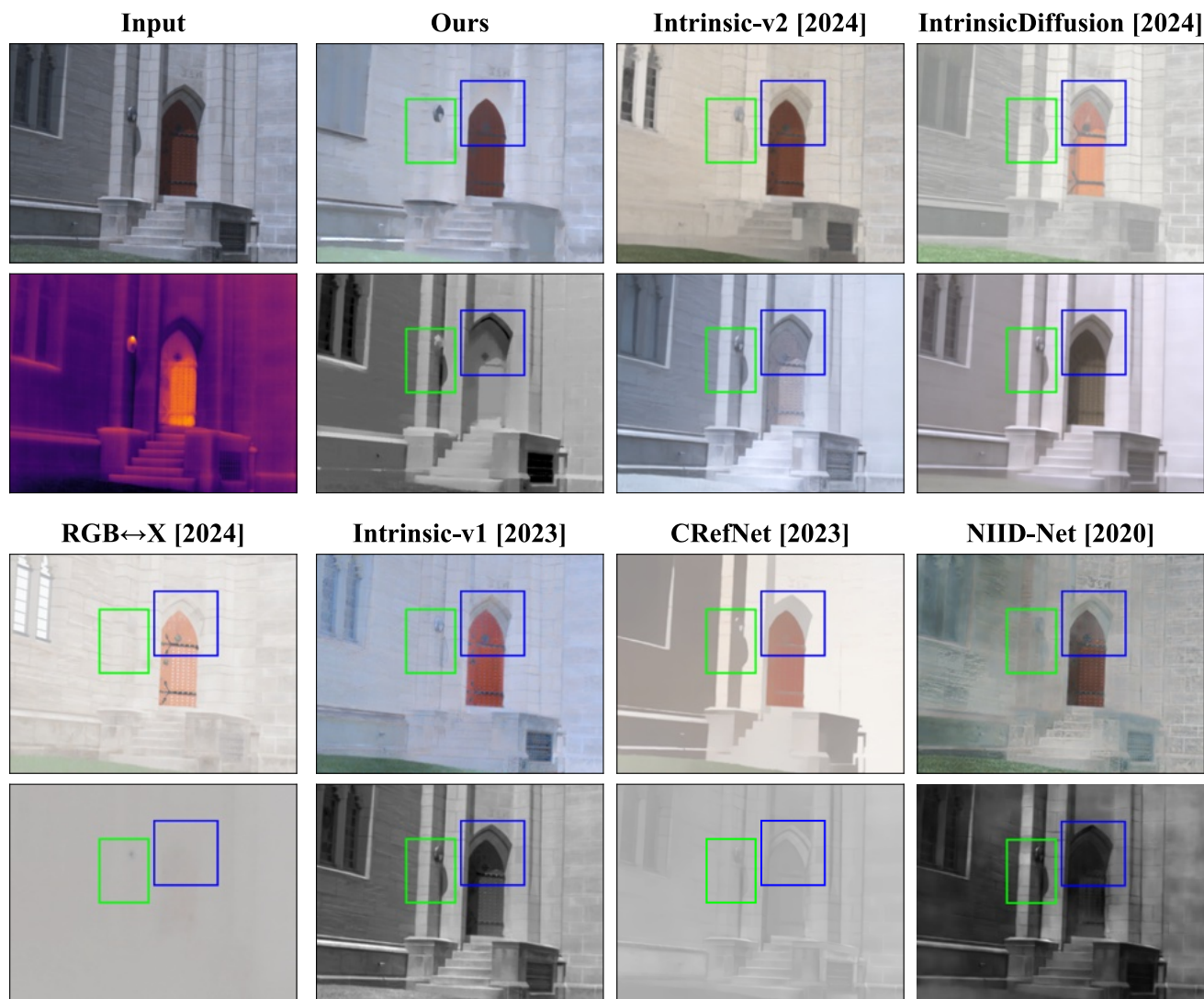


Figure 21. Qualitative comparisons to state-of-the-art baselines.



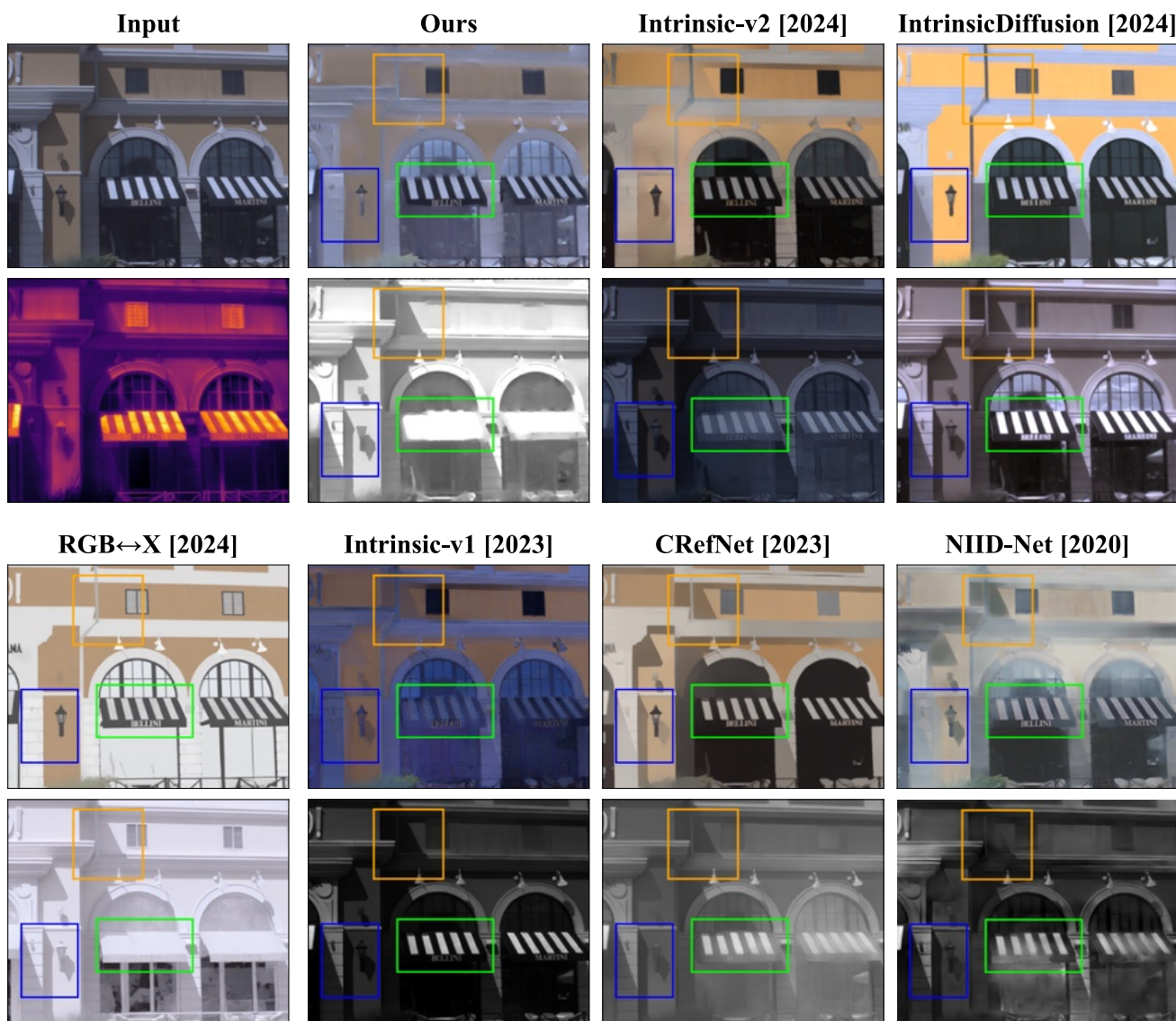


Figure 22. Qualitative comparisons to state-of-the-art baselines.

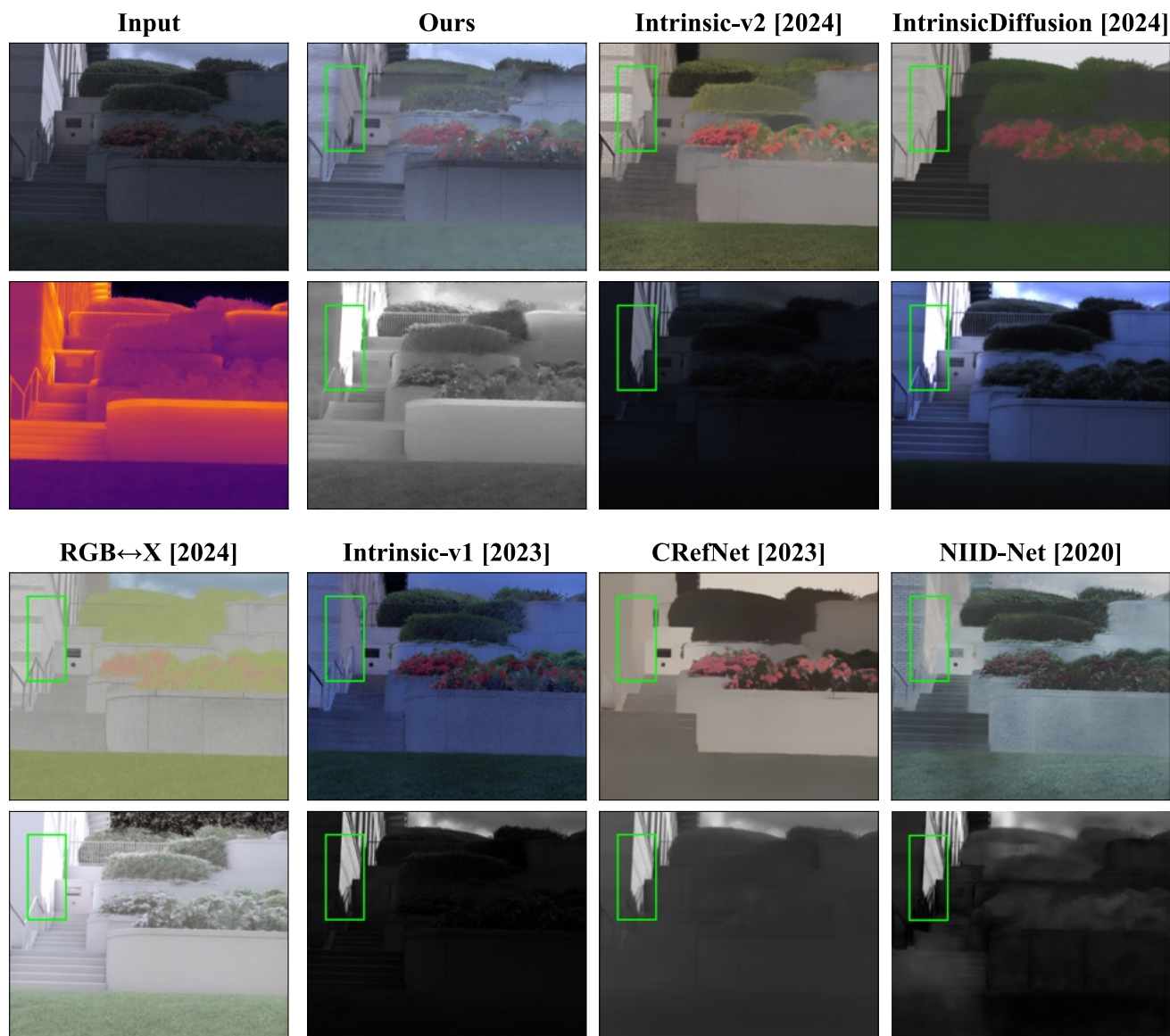


Figure 23. Qualitative comparisons to state-of-the-art baselines.

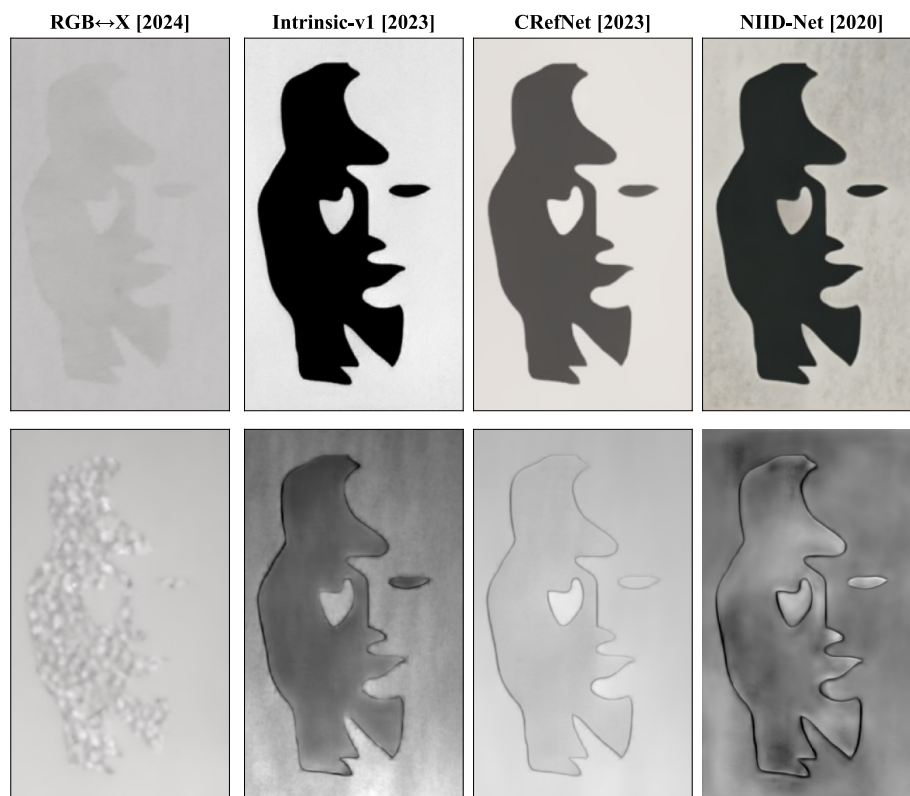
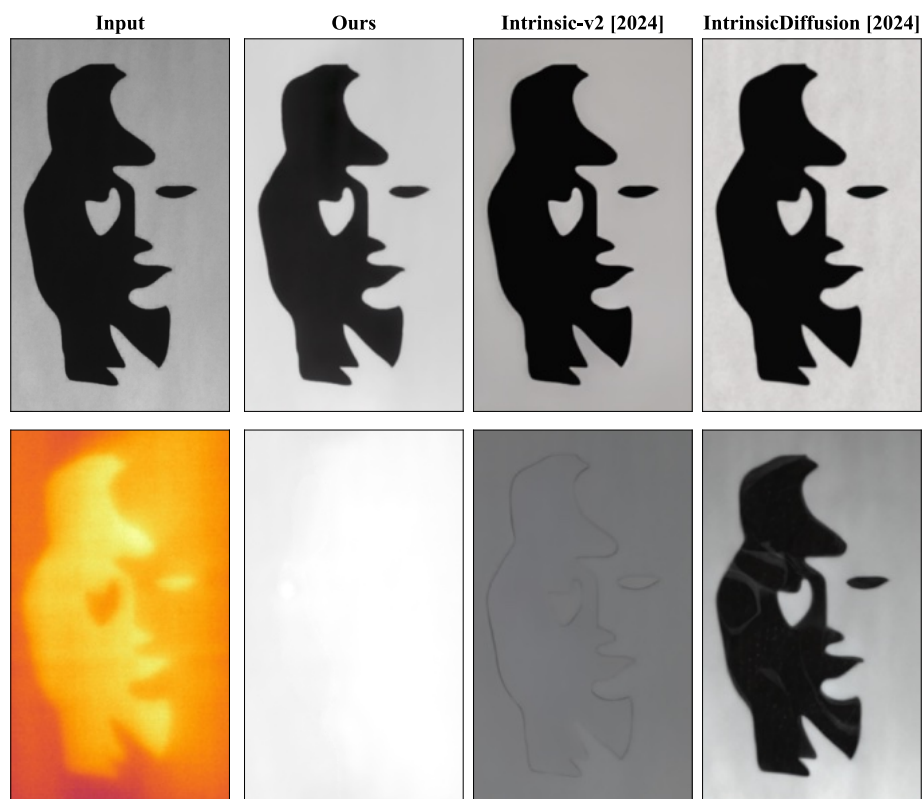


Figure 24. Qualitative comparisons to state-of-the-art baselines on a printed image.



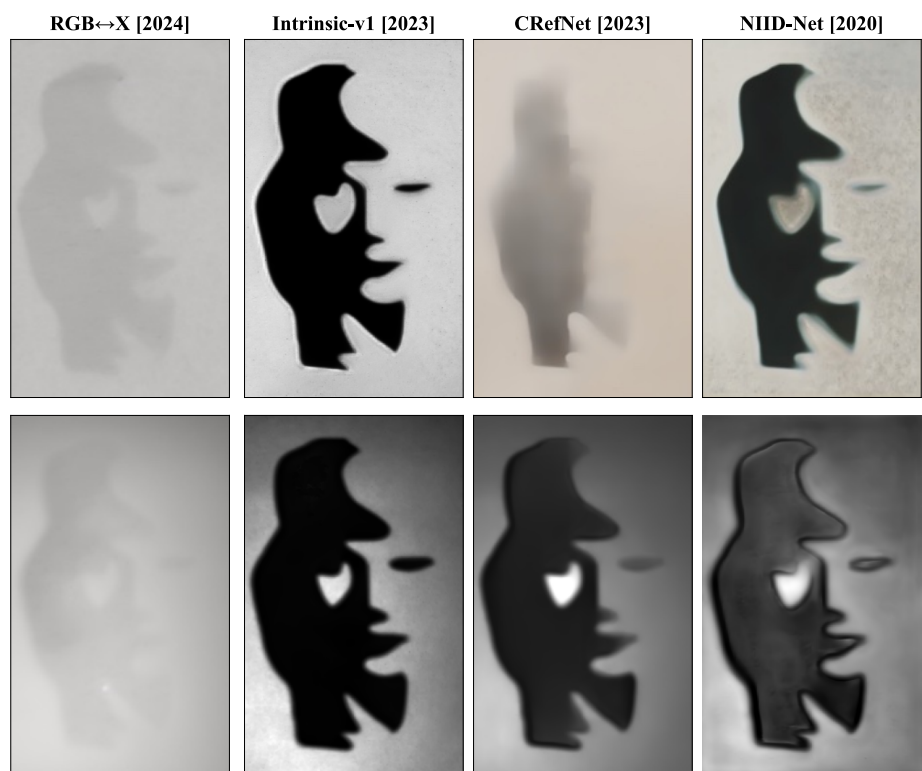
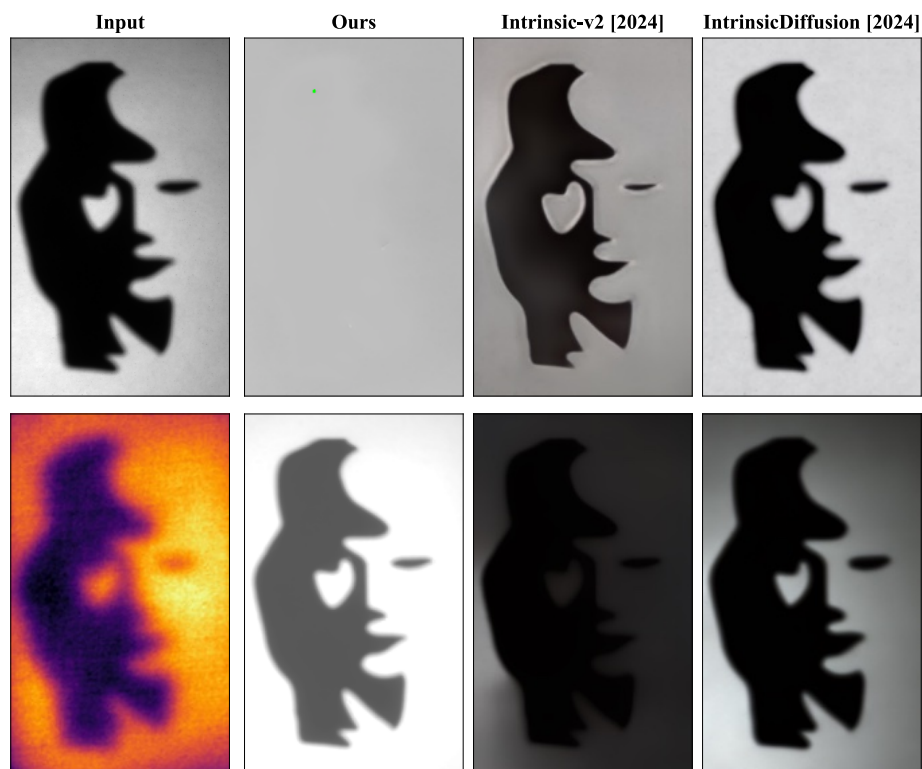


Figure 25. Qualitative comparisons to state-of-the-art baselines on a projected image.